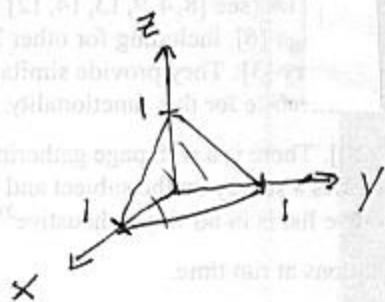


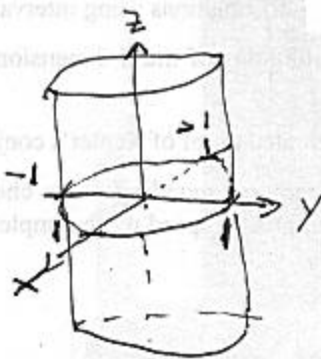
- (1) (a) an ellipsoid, (b) a plane, (c) a circular cylinder with z -axis as axis
(d) a paraboloid, (e) a hyperboloid of ^{one} sheet with axis equal to the z -axis

(2)

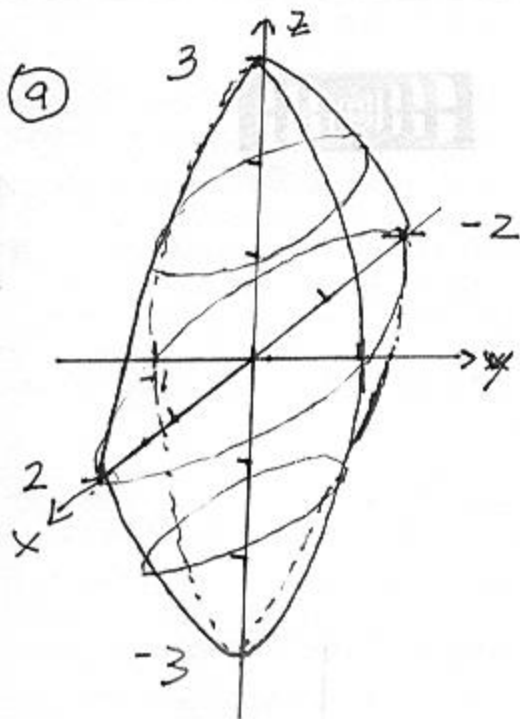
(b)



(c)



(a)



(3) The general form is

$$z - z_0 = m(x - x_0) + n(y - y_0)$$

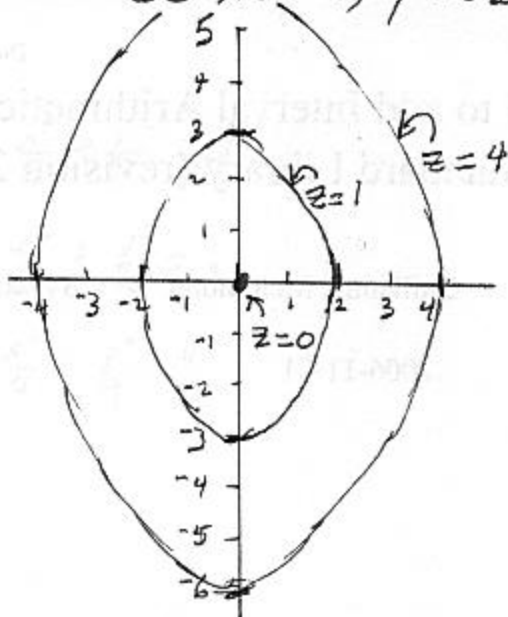
$(x_0, y_0, z_0) = (0, 0, 1)$, $m = -1$, $n = -1$, so the equation is:

$$z - 1 = -x - y, \text{ i.e. } x + y + z = 1, \text{ or } \boxed{z = 1 - x - y}.$$

(4) $z = 0$: $\frac{x^2}{4} + \frac{y^2}{9} = 0$, the origin $(0, 0)$

$z = 1$: $\frac{x^2}{4} + \frac{y^2}{9} = 1$, an ellipse intersecting the axes at $x = \pm 2$, $y = \pm 3$.

$z = 4$: $\frac{x^2}{4} + \frac{y^2}{9} = 4$, an ellipse intersecting the axes at $x = \pm 4$, $y = \pm 6$.



(5) The function is defined except on the diagonal line $y = -x$ where f is defined

$$f(x, y) = \frac{x^3 + y^3}{x + y} = x^2 - xy + y^2 \rightarrow 0 \text{ as } (x, y) \rightarrow (0, 0)$$

Hence, $\lim_{(x, y) \rightarrow (0, 0)} f(x, y) = 0$.